

## chain-consistent-effective-continuity<sup>13,45</sup>

$\forall es:\text{ES}, Cmd:\text{Type}, In:\text{AbsInterface}(Cmd), isupdate:(Cmd \rightarrow \mathbb{B}), Sys, Out:\text{AbsInterface}(\text{Top}).$   
 $(E(In) \subseteq_r E(Sys))$   
 $\Rightarrow (E(Out) \subseteq_r E(Sys))$   
 $\Rightarrow (\forall f:\text{sys-antecedent}(es; Sys). (\forall e:E(In). f(e) = e \in E))$   
 $\Rightarrow (\forall chain:(E(Sys) \rightarrow (\text{Id List})).$   
chain-consistent( $f; chain$ )  
 $\Rightarrow (\forall x:E(Sys).$   
effective( $x$ )  
 $\Rightarrow (\forall e':E(In).$   
 $(\uparrow(isupdate(In(e'))))$   
 $\Rightarrow \text{loc}(x) << \text{loc}(e')$   
 $\Rightarrow (\exists e:E(Sys)$   
 $(\text{loc}(e) = \text{loc}(e') \in \text{Id} \ \& \ (\neg(\text{loc}(f(e)) = \text{loc}(e) \in \text{Id}) \ \& \ x \text{ is } f^*(e))))))$